

Second Hint for Problem 232

We can apply the formula of Problem 226 to get

$$\begin{aligned}\bigcup_{i=1}^n A_i &= \left| \left(\bigcup_{i=1}^{n-1} A_i \right) \cup A_n \right| \\ &= \left| \bigcup_{i=1}^{n-1} A_i \right| + |A_n| - \left| \left(\bigcup_{i=1}^{n-1} A_i \right) \cap A_n \right| \\ &= \left| \bigcup_{i=1}^{n-1} A_i \right| + |A_n| - \left| \bigcup_{i=1}^{n-1} A_i \cap A_n \right| \quad (*)\end{aligned}$$